

# Pseudo Three-Dimensional Modeling of Particle Fuel Packing Using Distinct Element Method

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## 1. INTRODUCTION

### ⊕ FBR cycle system

Low-decontaminated MA fuel is to be used.

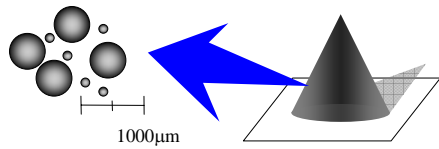
**Vibro-filling fuel** is suitable.

- Because...
1. Simple manufacturing
  2. Good remote handling
  3. Low cost

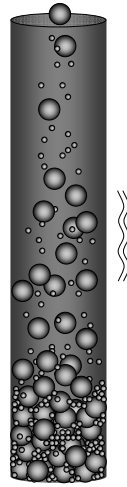
**Sphere-pac Fuel**  
Vipac Fuel

### ⊕ Sphere-pac fuel manufacturing

1. MOX fuel is formed to be spherical. (About 10 $\mu$ m~1000 $\mu$ m)



2. Particle-fuel is filled in a cladding tube under a vibrational motion. Two kind of particle of different diameter are blended and packed.



### ⊕ Challenging of sphere-pac fuel

For achieving **HIGH** and **UNIFORM** packing density

1. Comprehending the behavior of particles in a vibrating tube
2. Estimating the most effective value

We apply a Distinct Element Method (DEM) to numerical simulation of the vibration-based packing process

### In 2-D simulation...

- Low computational cost
- × Infiltration of particles

### In 3-D simulation...

- × Significant computational cost
- Infiltration of particles

**We propose a pseudo three-dimensional simulation method.**

- Practical computational cost
- Infiltration of particles can be expressed

## 2. COMPUTATIONAL METHOD

### ⊕ Two-Dimensional Distinct Element Method

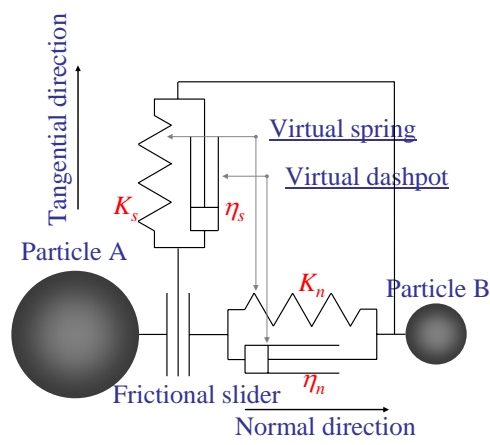
To calculate a contact force...

**Virtual spring** and **Virtual dashpot** are assumed.

A repulsion force and A friction force

An energy dissipation

Contact Force can be expressed.



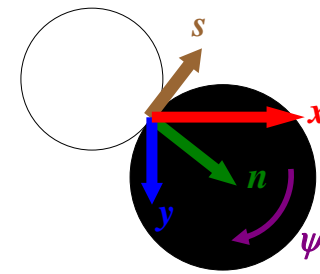
The Voigt model of contact force between two particles

$$F_n = \eta_n \frac{du_n}{dt} + K_n u_n$$

$$F_s = \eta_s \left( \frac{du_s}{dt} + r \frac{d\psi}{dt} \right) + K_s (u_s + r\psi)$$

Normal direction ( $n$ )  
Tangential direction ( $s$ )  
Horizontal direction ( $x$ )  
Vertical direction ( $y$ )  
Rotational direction ( $\psi$ )

Summation of all contact particles force



### NOMENCLATURE

$F$ ; contact force  
 $K$ ; a stiffness coefficient  
 $\eta$ ; a damping coefficient  
 $u$ ; relative displacement  
 $\psi$ ; displacement of relative rotation  
 $m$ ; mass of particles  
 $I$ ; inertia moment  
 $n$ ; the number of contact particles

### Newton's equation of motion

$$m \frac{d^2 x}{dt^2} = \sum_{j=1}^n F_{xj}$$

$$m \frac{d^2 y}{dt^2} = \sum_{j=1}^n F_{yj} - mg$$

$$I \frac{d^2 \psi}{dt^2} = \sum_{j=1}^n r F_{\psi j}$$

### ⊕ Pseudo Three-Dimensional Model

Particles of the same diameter

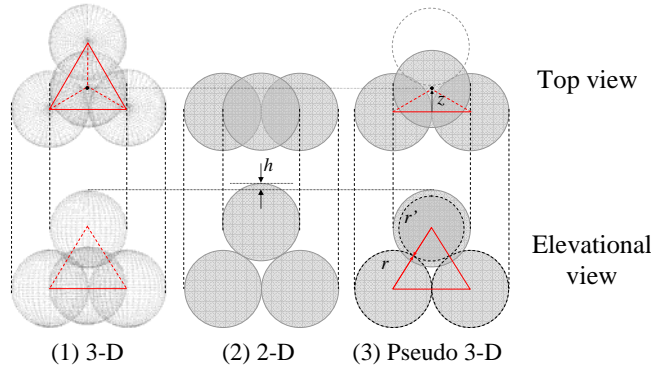
3-D closest packed structure  $\neq$  2-D closest packed structure

In Pseudo 3-D model...

Equivalent diameter  $r'$  is defined

For judging whether particles are in contact each other or not

$$\begin{cases} r' = \left( \sqrt{\frac{11}{3}} - 1 \right) r \\ h = \left( \sqrt{3} - \sqrt{\frac{8}{3}} \right) r \\ z = \frac{1}{\sqrt{3}} r \end{cases}$$



(1) 3-D (2) 2-D (3) Pseudo 3-D

Particles of different diameter

In 3-D simulation...

A fine particle **can** pass through the opening space between coarse particles.

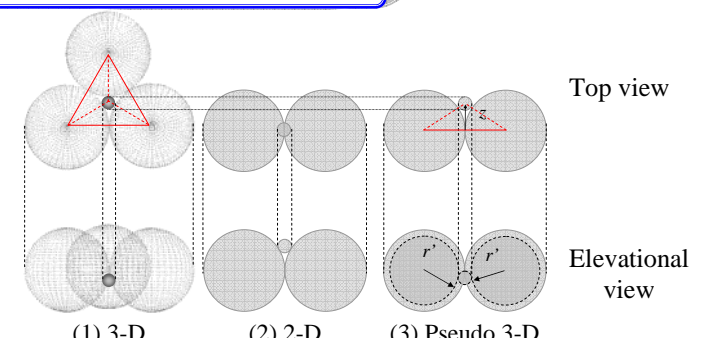
In 2-D simulation...

A fine particle **cannot** pass through the opening space between coarse particles.

In Pseudo 3-D model...

Equivalent diameter  $r'$  is defined

$$\begin{cases} r' = \left( 1 - \frac{2\sqrt{3}-3}{6} \right) r \\ z = \frac{1}{\sqrt{3}} r \end{cases}$$

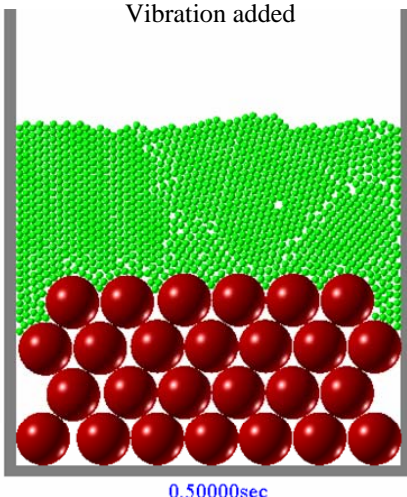


(1) 3-D (2) 2-D (3) Pseudo 3-D

## 3. NUMERICAL SIMULATION

### Two-dimensional simulation

Vibration added

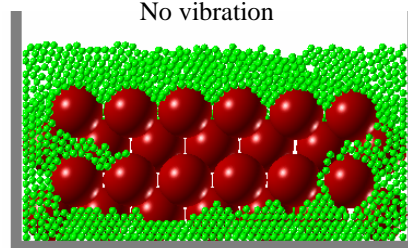


0.50000sec

No infiltration of particles due to 2-D simulation

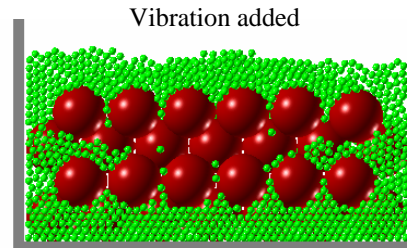
### Pseudo three-dimensional simulation

No vibration

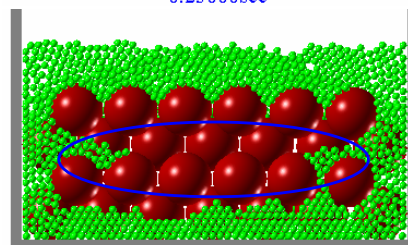


0.25000sec

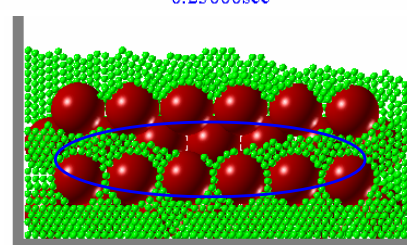
Vibration added



0.25000sec



0.50000sec



0.50000sec

Realistic analysis of fuel packing phenomenon  
Enhancement of the infiltration due to external vibration

### The condition of analysis

particles	
coarse particles diameter	1.40E-3 [m]
fine particles diameter	2.00E-4 [m]
density	1.10E+4 [kg/m <sup>3</sup> ]
Young's modules	1.00E+10 [Pa]
Poisson's ratio	0.28 [-]
coefficient of friction	0.25 [-]
number of coarse particles	26
number of fine particles	1200
container	
width	1.00E-2 [m]
height	2.00E-2 [m]
Young's modules	3.90E+9
Poisson's ratio	0.25
coefficient of friction	0.17
calculation	
time step size	1.0E-7 [sec]
duration time	0.5 [sec]
vibration	
amplitude	2.50E-5 [m]
frequency	200 [Hz]

**The dynamic behavior of particles in the manufacturing process of the sphere-pac fuel can be simulated with the present methodology.**